

## MOLECULAR INTERACTIONS IN BIOLOGICAL SYSTEMS.

III<sup>4</sup>. THE SIBIS AND HIBIS PROGRAMS. APPLICATIONS.

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Summary. The SIBIS and HIBIS programs implement our algorithms developed to quantify the steric (SIBIS) and hydrophobic (HIBIS) interactions in biological systems. The paper presents the flowcharts, the complete listing in FORTRAN of the programs, and details the structure of the input/output data. Illustratively, one performs SIBIS and HIBIS calculations for a serie of twenty inhibitors (triazines) of *L.casei* dehydropholate reductase, good results being reported. Finally, the algorithm CONEX, which teaches the computer to recognize connected graphs, is given.

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### 1. The SIBIS and HIBIS Programs

The two algorithms (SIBIS - Steric Interactions in Biological Systems and HIBIS - Hydrophobic Interactions in Biological Systems) were discussed and applied to drug - receptor interactions in previous papers (i.e., refs. 1-3, and 4, respectively).

The present paper contains the flowchart, the complete listing of the programs and the structure of the input/output data. An application of these algorithms to a serie of twenty inhibitors of *L.casei* dihydropholate reductase is also given.

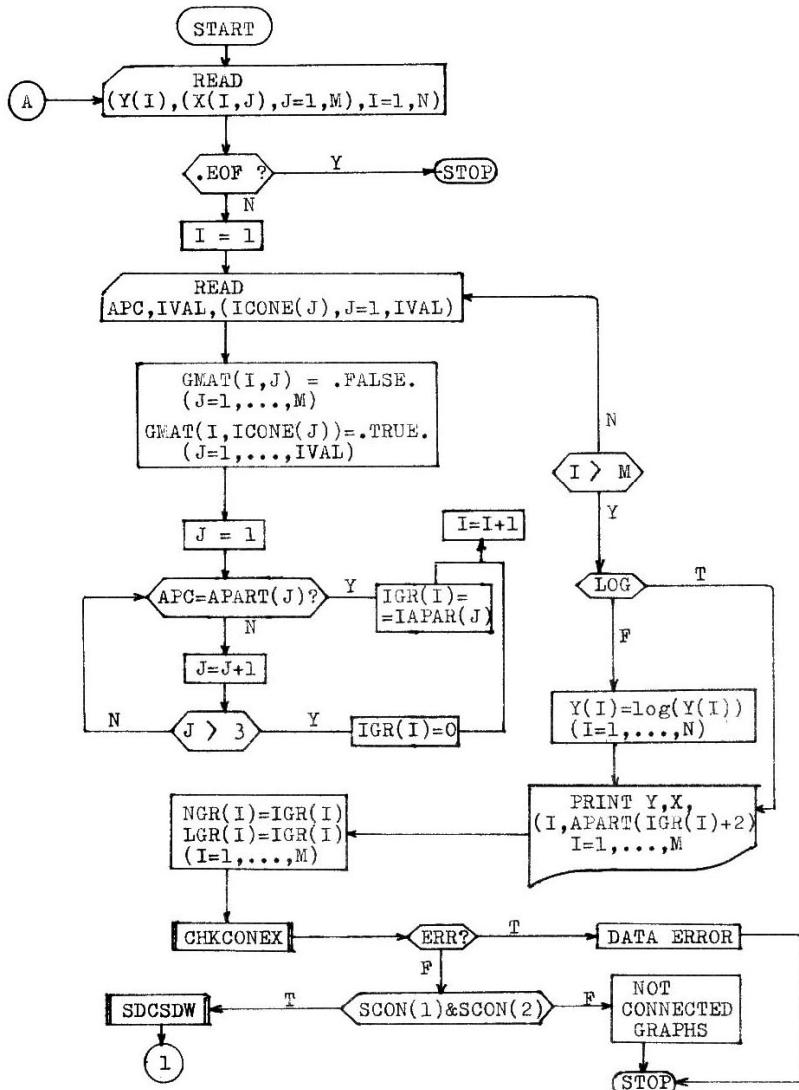
The main difference between SIBIS and HIBIS consists in the objective functions to be optimized, namely:

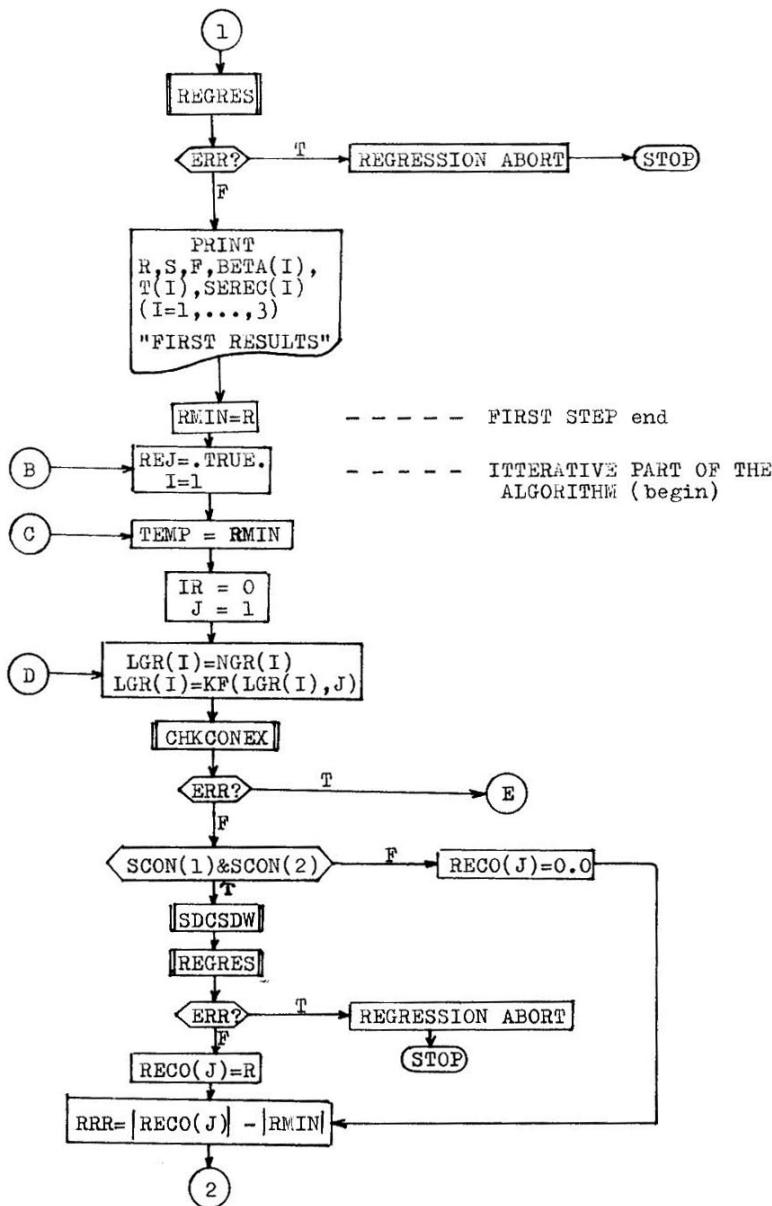
$$BR = a + b SD_c^x + c SD_w^x \quad (\text{SIBIS})$$

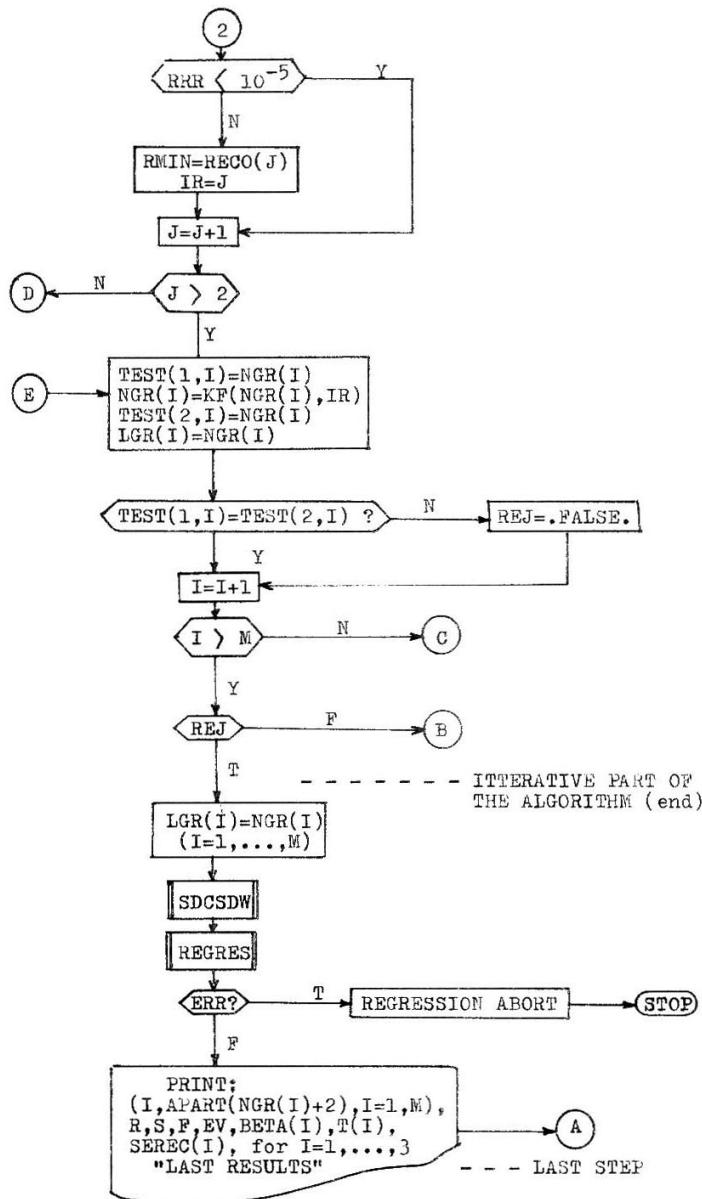
$$BR = m + n f + p f^2 \quad (\text{HIBIS})$$

(BR stands for the Biological Response). The mathematical tool is the same (i.e., the least squares technique with the subsidiary condition to preserve connected some subgraphs of the  $\langle IRS \rangle$  (Investigated Receptor Space) graph). Accordingly, the SIBIS and HIBIS programs have the same flowchart given below. The complete listing of the programs is given in Appendix 1. Appendix 2 contains the algorithm CONEX, which teaches the computer to recognize connected graphs.

SIBIS and HIBIS - the flowchart







The structure of the input data is detailed below.

The SIBIS and HIBIS programs together with the POLYREG program (which performs multivariate regressive analysis) are parts of a unique program called "ABSIN" (Analysis of Biological Structures INteractions).

Input data for this program are composed from an unlimited number of specific input data for each of its parts. One can select the subprogram by a Keyword, namely: SIBIS-LV (SIBIS - Linear Version), SIBIS-NL (SIBIS - Non Linear version), HIBIS, and POLYREG.

A commented example of input data is given at the end of Appendix I .

## 2. Applications

The  $I_{50}$  values for the inhibition of *L.casei* dihydropholate reductase by triazines of type I are taken from ref. 5 (see Table 1).

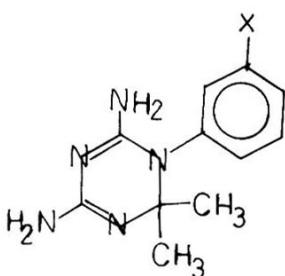


Fig.1.

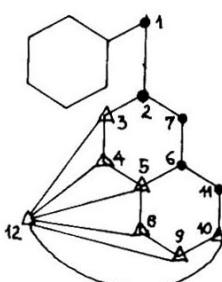


Fig.2.

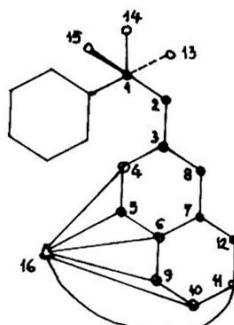


Fig.3.

The starting  $\langle IRS \rangle$  for SIBIS calculations is

$$\langle \text{IRS} \rangle_S^{\text{init}} = [c(1-3, 7, 8, 11, 12); w(4-6, 9, 10, 13-15); i(16)]$$

(see Figure 1; c-type subgraph corresponds to the structure of compound 20 from Table 1). - Explanations for the significance of c, w, r and i are given in refs. 1 and 4 -.

The starting  $\langle \text{IRS} \rangle$  for HIBIS calculations is

$$\langle \text{IRS} \rangle_H^{\text{init}} = [r(1, 2, 6, 7, 11); i(3-5, 8, 9)]$$

(see Figure 2). The two optimization algorithms offer the following results:

$$\langle \text{IRS} \rangle_S^{\text{opt}} = [c(1-5, 7, 8, 11, 12); w(6, 9, 10, 13-15); i(16)]$$

$$\begin{aligned} \log 1/I_{50} = & 2.964(\pm 0.098) + 0.261(\pm 0.030)SD_c^{\text{opt}} - \\ & (t=30.383) \quad (t=8.787) \\ & - 0.382(\pm 0.082)SD_w^{\text{opt}} \\ & (t=4.674) \end{aligned} \quad (1)$$

( $r = 0.789$ ,  $s = 0.413$ ,  $F = 8.801$ ), and, respectively,

$$\langle \text{IRS} \rangle_H^{\text{opt}} = [r(1-7, 10, 11); i(8, 9, 12)]$$

$$\begin{aligned} \log 1/I_{50} = & 3.017(\pm 0.088) + 0.368(\pm 0.060)f + \\ & (t=34.227) \quad (t=6.137) \\ & + 0.031(\pm 0.023)f^2 \\ & (t=1.340) \end{aligned} \quad (2)$$

( $r = 0.832$ ,  $s = 0.373$ ,  $F = 11.987$ )

One may combine the equations (1) and (2) into one equation, resulting the equation

$$\begin{aligned} \log 1/I_{50} = & 2.963(\pm 0.079) + 0.143(\pm 0.024)SD_c^{\text{opt}} - \\ & (t=37.393) \quad (t=5.926) \\ & - 0.228(\pm 0.066)SD_w^{\text{opt}} + 0.276(\pm 0.056)f \\ & (t=-3.445) \quad (t=4.883) \end{aligned} \quad (3)$$

( $r = 0.875$ ,  $s = 0.325$ ,  $F = 12.266$ )

The  $f^2$  term has been rejected because it is not statistically significant (i.e.  $t_{19,0.05} = 2.093 > 1.340$ ).

Table 1. Inhibition constants for the inhibition of *L.casei* DHFR by Triazines of type (I)

No.	X	$\log 1/I_{50}$	$SD_c^*$	$SD_w^*$	$\sum f_i$
1	$SO_2NH_2$	1.82	2.2	2.0	-1.480
2	$CONH_2$	2.47	2.0	1.0	-1.109
3	H	2.64	0.0	0.0	0.167
4	$COCH_3$	2.87	2.0	1.0	-0.115
5	$CH_3$	3.07	1.0	0.0	0.691
6	$OCH_3$	3.12	2.0	0.0	0.262
7	OH	3.19	1.0	0.0	-0.309
8	$C(CH_3)_3$	3.20	2.0	2.0	2.150
9	$COOC_2H_5$	3.21	4.0	1.0	0.975
10	$SO_2F$	3.21	2.0	2.0	-1.488
11	F	3.29	0.8	0.0	0.382
12	$CF_3$	3.29	1.8	1.6	1.323
13	Cl	3.45	1.2	0.0	0.925
14	$NO_2$	3.56	2.0	1.0	-0.066
15	Br	3.69	1.3	0.0	1.121
16	I	3.73	1.7	0.0	1.430
17	$O(CH_2)_2OC_6H_5$	3.74	7.0	3.0	1.574
18	$OCH_2C_6H_5$	4.20	7.0	1.0	2.163
19	$O(CH_2)_3CH_3$	4.20	5.0	0.0	1.846
20	$(CH_2)_5CH_3$	4.96	6.0	0.0	3.295

References

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3. I.Motoc, Can.J.Pharm.Sci., in press
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5. R.J.A.Walsh, K.R.H.Wooldridge, D.Jackson and J.Gilmour, Eur.J.Med.Chem., 12, 495 (1977).

APPENDIX 1

```
*****  
*          SSSS  II  BBBB  II  SSSS  
*          SS    II  BB  B  II  SS  
*          SS    II  BBBB  II  SS  
*          SS  SS  II  BB  B  II  SS  
*          SSSS  II  BBBB  II  SSSS  
*****
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* SEGMENT GRAMAT, VALORI, REGPAR  
COMMON /GRAMAT/, VALORI, REGPAR  
COMMON /VALURI/, X(100,50), Y(100), IGR(50), NGR(50), LGR(50)  
1 SCON(3), SD(100,3), TEST(2,50), NM  
COMMON /REGPAR/, BETA(21), F(21), SEREC(21), R, S, F, EXPVAR  
1, SEHY, SERES  
2, VEPS  
  
C      DIMENSION  ICONE(50)  
DIMENSION  RECn(2)  
DIMENSION  TIT(20), FRD(20), FWR(20)  
DIMENSION  MARK(50)  
DIMENSION  APART(3)  
DIMENSION  TAPAR(3)  
DIMENSION  EG(3)  
INTEGER  CHOICE(2), STDCH(2,4)  
DOUBLE PRECISION BETA, VEPS  
LOGICAL  AVY, AVX, AVIGR  
LOGICAL  MARK, MRK  
LOGICAL  GMAT, WMAT, REJ, SCON, NPRINT, LOG  
LOGICAL *1 ERR  
LOGICAL *1 EG  
INTEGER  TEST, DOI  
INTEGER  CR, LP  
DATA CR /105/  
DATA LP /108/  
DATA NMAX, MMAX, NPRINT, DOI / 100, 50, .TRUE., 2 /  
DATA APART, TAPAR / 'CT', 'I', 'W', '=-', '0,1', '/' /  
DATA REC, CAV / 'R', 'C', '/' /  
DATA STDCH / 'HIBI', 'S', 'SIBI', 'S-LV', 'SIBI', 'S-NL', 'POLY',  
1, REG / /  
C      KF(IND1,IND2) = MOD ((IND1 + 1 + IND2), 3) -1  
C      VEPS = 0.1D-71
```

```
LMX = 60
IPAG = 1
CONTINUE
100 READ(CR,200,END=990) CHOICE, AVY, AVX, AVIGR
DO 110 I = 1, 4
    IF(CHOICE(J),NE, STDCH(J,I)) GOTO 110
CONTINUE
INDRUN = I
GOTO 111
110 CONTINUE
WRITE(1P,113) CHOICE
STOP 'WRONG CHOICE PARAMETER'
111 CONTINUE
112 FORMAT('1',10X,12('1')/11X,'1',2A4,'1'/11X,12('1'),10X,
113 1'PAG,1,15//11X,10A4/11X,10A4//')
FORMAT('//11X,2A4/11X,7('1')/')
IF (INDRUN,NE, 4) GOTO 114
CALL POLYREG
GOTO 100
114 CONTINUE
IF (INDRUN .GT. 2) GOTO 115
IRUN = 2
IRN = 3
GOTO 116
115 IRUN = 3
IRN = 4
116 CONTINUE
IF (INDRUN, EQ, 1) GOTO 117
APARI(1) = CAV
GOTO 118
117 APARI(1) = REC
CONTINUE
ITER = 0
IF(.NOT.(AVY, OR, AVX, OR, AVIGR)) GOTO 610
READ(CR,2,END=1000) TITL
DO 1/ I = 1, 3
    MARK(I) = ,FALSE,
17 CONTINUE
MRK = TRUE
READ(CR,1,END=1000) N,M,LOG
1 FORMAT (I3,I2,L1)
IF(N.GT.NMAX) GOTO 2000
IF(M.GT.MMAX) GOTO 2000
WRITE(1P,112) CHOICE, IPAG, TITL
IPAG = IPAG + 1
READ(CR,2) FWR
PRINI = 20
2 FORMAT(20A4)
FORMAT(2A4,3L1)
20 FORMAT(11X,'** VECTOR <Y> AND MATRIX <x>!//')
21 FORMAT (I2,A1,(38I2))
25 FORMAT(11X,
11VEIEX,I3,',',A1,'> CONNECTION!',(I38,10(I3,!,!)))
IF (.NOT., AVY) GOTO 253
READ(CR,2) FRD
READ(CR,FRD) (Y(I),I=1,N)
C
IF ( LOG ) GOTO 61
DO 6 I = 1, N
    Y(I) = ALOG10(Y(I))
61 CONTINUE
IF (.NOT., AVX) GOTO 305
READ(CR,2) FRD
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3      READ (CR,FRD,END=305) T, (X(I,J), J = 1, M)
IF (I .GT. N) GOTO 2012
GOTO 3
305  CONTINUE
DO 30 I = 1, N
      WRITE (LP,FWR) Y(I),(X(I,J),J=1,M)
30    CONTINUE
IF (.NOT. AVIGR) GOTO 610
WRITE (LP,112) CHOICE, IPAG, TITL
IPAG = IPAG + 1
PRINI 31
FORMAT(//11X, '** CONNECTIVITY MATRIX **//)
READ(CA,21,END=5) I, APC, IVAL, (ICONE(J), J = 1, IVAL)
PRINI 25,I,APC,(ICONE(J),J=1,IVAL)
IF ('I' .GT. M) GOTO 2016
DO 4 J = 1, M
GMAT(I,J) = .FALSE.
DO 41 J = 1, IVAL
GMAT(I, ICONE(J)) = .TRUE.
CONTINUE
DO 42 J = 1, 3
      IF (APC .NE. IAPART(J)) GOTO 42
      IGR(I) = IAPAR(J)
      MRK(I) = .TRUE.
GOTO 32
42  CONTINUE
IGR(I) = 0
GOTO 32
5    CONTINUE
DO 51 I = 1, M
      IF ( MARK(I) ) GOTO 51
      MRK = .FALSE.
51  CONTINUE
IF ('MRK') GOTO 52
WRITE (LP,510)
510 FORMAT(//11X,'WRONGLY PARAMETRIZED IGR')
GOTO 100
52  CONTINUE
C
610  CONTINUE
C
      WRITE (LP,112) CHOICE, IPAG, TITL
IPAG = IPAG + 1
PRINI 77,(I,APART(IGR(I)+2),I=1,M)
C
DO / I = 1, 4
NGR(I) = IGR(I)
LGR(I) = IGR(I)
71  FORMAT(//11X,'RESULTS OF THE FIRST REGRESSION!//')
72  FORMAT(//11X,'R =',F7.5, ', S =',F7.5, '(-) //'
1'; r =',F9.3, ', EV =',F7.4/11X,5'(-) //'
212X,'----- BETA(I) ----- T(I) ----- ERR.(I) //'
312X,'----- ----- ----- ----- //')
720 FORMAT(11X,12,3F11.3)
73  FORMAT(//11X,'RESULTS OF THE LAST REGRESSION!//')
75  FORMAT(//11X,'RESULTS FOR ITERATION NO.',I5//)
C
CALL CHKCONE (ERR, EG)
C
IF (EMR .AND. (INDRUN,NE,1)) GOTO 76
IF ((INDRUN,EN,1) .AND. .NOT. EG(3)) GOTO 2100
IF ((INDRUN,EN,1) .AND. (EG(1).OR. EG(2))) GOTO 76
C
IF (.NOT. (SCON(1) .AND. SCON(2))) GOTO 2010
```

```
C      CALL SDCCSW(INDRUN)
C      CALL REGRES(Y, SD, N, IRUN, NPRINT, ERR)
C      IF ( ERR ) GOTO 1050
C
C      PRINT 71
C      PRINT 72, R, S, F, EXPVAR
C      DO 150 I = 1, IRN
C          14   I = 1
C          PRINT 720, IZ, BETA(I), T(I), SEREC(I)
C      CONTINUE
C      RMIN = R
C
C      GOTO 8
76     WRITE(LP, 760)
760    FORMAT(//11X,'*DATA ERROR* - CHECK THE DATA SET')
C      GOTO 100
77     FORMAT(//11X,'INITIAL PARTITION OF THE GRAPH IS:',// 
C(11X/5(I6,1->1,A1,2X)))
78     FORMAT(//11X,'FINAL PARTITION OF THE GRAPH IS:',// 
C(11X/5(I6,1->1,A1,2X)))
C
8      REJ = .TRUE.
C      ITER = ITER+1
C
C      DO 170 I = 1, M
C      TEMP = RMIN
C      IR = 0
C
C      DO 13 J = 1, 2
C
C      LGR(I) = NGR(I)
C      LGR(I) = KF( LGR(I), J )
C
C      IF(INDRUN .GT. 1) GOTO 800
C      IF(LGR(I) .EQ. 1) GOTO 13
800    CONTINUE
C
C      CALL CHKCONE(X, ERR, EG)
C
C      IF( (ERR AND (INDRUN .NE. 1)) GOTO 131
C      IF((INDRUN.EQ.1).AND.(NOT EG(3))) GOTO 2100
C      IF((INDRUN.EQ.1).AND.(EG(1).OR. EG(2))) GOTO 11
C      IF ( .NOT. (SCON(1) .AND. SCON(2)) ) GOTO 11
C      CALL SDCCSW(INDRUN)
C      CALL REGRES(Y, SD, N, IRUN, NPRINT, ERR)
C      IF ( ERR ) GOTO 1050
C      RECO(J) = R
C      GOTO 12
11     RECO(J) = 0.0
12     RRR = ABS(RECO(J)) - ABS(RMIN)
C      IF ( RRR .LT. 0.00001 ) GOTO 13
C      RMIN = RECO(J)
C      IR = J
C
13     CONTINUE
C
131    CONTINUE
C
C      TEST(1,I) = NGR(I)
C      NGR(I) = KF( NGR(I), IR )
```

```
      TESI(2,I) = NGR(I)
      LGR(I) = NGR(I)
C      CONTINUE
15      DO 10 I = 1, M
C      IF (TEST(1,I) .NE. TEST(2,I) ) REJ = .FALSE.
C      CONTINUE
16      IF ( .NOT. REJ ) GOTO 8
C      DO 9 J = 1, M
9      LGR(J) = NGR(J)
C      CALL SDCSDW(INDRUN)
C      CALL REGRES(Y, SD, N, IRUN, NPRINT, ERR)
C      IF ( ERR ) GOTO 1050
C      PRINI 79,ITER
79      FORMAT(//,11X,I4,' ITTERATIONS PERFORMED'//)
C      PRINI 78,(I,APART(NGR(I)+2),I=1,M)
C      PRINT 73
C      PRINT 72,R,S,F,EXPVAR
C      DO 980 I = 1, IRN
C      IZ = I - 1
C      PRINI 720, IZ, BETA(I), T(I), SEREC(I)
C      CONTINUE
980      GOTU 100
990      CONTINUE
1000      STOP ' OUTPUT OK'
1050      WRITE(LP, 1051)
      GOTU 100
1051      FORMAT(//11X, 'ABANDONED RUN'//)
2000      WRITE(LP, 2001)
      GOTU 100
2001      FORMAT(//11X, 'WRONG <N> OR <M>'//)
2010      WRITE(LP, 2011)
      GOTU 100
2011      FORMAT(//11X, 'NOT CONNECTED GRAPHS'//)
2016      WRITE(LP,2018)
2013      READ(CR,END = 100) TITL
      GOTU 2015
2014      FORMAT(//11X,'WRONG INDEX,IN --- <X>'//)
2012      WRITE(LP,2014)
2017      READ(CR,END = 100) TITL
      GOTU 2017
2018      FORMAT(//11X,'WRUNG INDEX,IN --- <IRS>'//)
C
2100      WRITE(LP, 2101)
2101      FORMAT(//11X,'WRONG <IRS>')
      GOTU 100
      END
* SEGMENT KEGPAR
*****
*      PPPPP    0000   LL    YY    Y    RRRRR    EEEEEEE   GGGG
*      PP      P  00    0   LL    YY    Y    RR    R    EEE    GG  G
*      PP      P  00    0   LL    YYY   Y    RR    R    EEE    DD
*      PPPPP    00    0   LL    YY    Y    RRRRR    EEEEEEE   GG  GGG
*      PP      00    0   LL    YY    Y    RR    R    EEE    GG  GGG
C      *      0000    LLLLLL  YY    RR    RR    EEEEEEE   GGGG  *
```

```
*  
*****  
C C C  
C SUBROUTINE POLYREG  
C COMMON /REGPAK/ BETA(21),T(21),SEREC(21)  
C 1,R,S,F,EXPVAR,SERYX,SERES  
C 2,VEPS  
C INTEGER IY,IX(20),KY,KX(20),CR  
C INTEGER*4 NMAX(2,21),NYNA(2)  
C REAL X(100,21),YMAN(100),XMAN(100,20),FORM(20),TITLE(40)  
C DOUBLE PRECISION BETA,VEPS  
C LOGICAL*1 NPH,ERR,PLSZ  
C LOGICAL*1 CHKN  
C DATA NPH /.FALSE./  
C DATA NYNA /4HDEP.,4HYAR./  
C DATA CR,LP / 105, 108 /  
C DATA LINMAX / 55 /  
C IPAG = 1  
C READ(CR,2,END=100)TITLE  
C FORMAT(20A4)  
C 3 FORMAT(/21X,'INPUT DATA'/21X,10(''//)  
C 4 FORMAT('1'//,21X,11(''')/21X,11('' POLYREG ))  
C 1/21X,11(''')5X,(PAG,15//,(15X,20A4))  
C 5 READ(CR,6,END=1)NK,PLSZ,VEPS,VDLZ  
C/ PRINT(300,NK,PLSZ,VEPS,VDLZ  
C/ 300 FORMAT(/10X,13,I2,L1,2G12.6//)  
C 6 FORMAT(I3,I2,L1,2G12.6)  
C IF(N .GT. 100)GOTO 500  
C IF(K .GT. 20) GOTO 200  
C KPI = 4  
C READ(CR,7,END=205)((NAMX(I,J),I=1,2),J=1,KP1)  
C READ(CR,7)FORM  
C 7 FORMAT(20A4)  
C DO 9 I = 1, N  
C READ(CR,FORM,END=205)(X(I,J),J=1,KP1)  
C IF(.NOT. PLSZ) GOTO 9  
C DO 8 J = 1, KP1  
C IF(X(I,J) ,NE, 0.0) GOTO 8  
C X(I,J) = VDLZ  
C 8 CONTINUE  
C CONTINUE  
C NLIN = 9  
C WRITE(LP,4)IPAG,TITLE  
C IPAG = IPAG + 1  
C N1 = N - 1  
C DO 11 I = 1, N1  
C 11 = I + 1  
C DO 101 J = 11, N  
C 101 = 10 + M - 1, KP1  
C IF(X(I,M) ,NE, X(J,M)) GOTO 101  
C 10 CONTINUE  
C WRITE(LP,12)  
C NLIN = NLIN + 4  
C GOTO 13  
C 101 CONTINUE  
C 12 FORMAT(11X,'WARNING ! --> IDENTICAL POINTS'//)  
C 13 WRITE(LP,3)  
C NLIN = NLIN + 4  
C 14 FORMAT(L1,I2,21(I2,I1))  
C LMIN = 5  
C LMAX = 5  
C 15 IF(LMAX .GT. N) LMAX = N  
C IF(LMIN .GT. N) GOTO 22
```

```
IF ( NLIN .LE. LINMAX + KP1 - 2 ) GOTO 152
NLIN = 9
WRITE(LP,4)IPAG,TITLE
IPAG = IPAG + 1
152 CONTINUE
      WRITE(LP,18)(I,I = LMIN, LMAX)
      FORMAT(9X,'NAME\POINT',5(I3,8X))
      WRITE(LP,91)
      FORMAT(1X)
      FORMAT(1X,T10.2A4,2X,5G11.4)
      NLIN = NLIN + 5
      DO 21 J = 1, KP1
        WRITE(LP,19)(NAMX(I,J),I=1,2)
        X(I,J),I=LMIN,LMAX)
1,     NLIN = NLIN + 1
21   CONTINUE
      LMIN = LMIN + 5
      LMAX = LMAX + 5
      GOTO 15
22   WRITE(LP,23)
      FORMAT(1X,11X,'END OF INPUT DATA',11X,17('=-'))
      NRUN = 1
24   READ(CR,14,END=5) CHKN,LIM,KY,IY,(KX(I),IX(I),I=1,LIM)
      IF(KT.GT.KP1) GOTO 202
      IF(LIM.EQ.0) GOTO 202
      IF(KY.EQ.0) GOTO 202
      DO 27 I = 1, LIM
        IF(KX(I).GT. KP1) GOTO 202
        IF(KX(I).EQ. 0) GOTO 202
27   CONTINUE
      WRITE(LP,4)IPAG,TITLE
      IPAG = IPAG + 1
      WRITE(LP,26)NRUN
26   FORMAT(1X,11X,'RUN NO.',I4/11X,11('=-')//)
      NRE = N
      IN = IY + 1
      WRITE(LP,40)
      WRITE(LP,25)(NAMX(I,KY),I=1,2),IY
25   FORMAT(1X,' ',2A4,' = CONTROL INDEX >',I3)
40   FORMAT(1X,'VARIABLES USED IN THIS RUN; T')
41   FORMAT(1X,'X(',I2,T) ',2A4,' = CONTROL INDEX >',I3)
      J1 = KY
      GOTO 111,113,115,117,119,121,123,125,127,129, IN
111  DO 112 I = 1, N
      IF ( .NOT. CHKN ) GOTO 1110
      IF(X(I,J1).GT.0.0)GOTO 1110
      IF(NRE.GE.I) NRE = I + 1
      GOTO 39
1110 CONTINUE
      YMNC(I) = ALOG10( X(I,J1) )
112 CONTINUE
      GOTO 39
113  DO 114 I = 1, N
      YMNC(I) = X(I,J1)
114 CONTINUE
      GOTO 39
115  DO 116 I = 1, N
      YMNC(I) = X(I,J1) ** 2
116 CONTINUE
      GOTO 39
117  DO 118 I = 1, N
      YMNC(I) = X(I,J1) ** 3
118 CONTINUE
      GOTO 39
```

```
119 DO 120 I = 1, N
      YMAN(I) = X(I,J1) ** 4
120 CONTINUE
      GOTO 39
121 DO 122 I = 1, N
      IF (.NOT. CHKN ) GOTO 1210
      IF(X(I,J1).NE.0.0)GOTO 1210
      IF(NRE.GE. I) NRE = I - 1
      GOTO 39
1210 CONTINUE
      YMAN(I) = 1.0 / X(I,J1)
122 CONTINUE
      GOTO 39
123 DO 124 I = 1, N
      IF (.NOT. CHKN ) GOTO 1230
      IF(X(I,J1).NE.0.0)GOTO 1230
      IF(NRE.GE. I) NRE = I - 1
      GOTO 39
1230 CONTINUE
      YMAN(I) = 1.0 / X(I,J1) ** 2
124 CONTINUE
      GOTO 39
125 DO 126 I = 1, N
      IF (.NOT. CHKN ) GOTO 1250
      IF(X(I,J1).GT.0.0)GOTO 1250
      IF(NRE.GE. I) NRE = I - 1
      GOTO 39
1250 CONTINUE
      YMAN(I) = - ALOG10( X(I,J1) )
126 CONTINUE
      GOTO 39
127 DO 128 I = 1, N
      YMAN(I) = EXP( X(I,J1) )
128 CONTINUE
      GOTO 39
129 DO 130 I = 1, N
      YMAN(I) = EXP( -X(I,J1) )
130 CONTINUE
      GOTO 39
CONTINUE
DO 55 J = 1, LIM
      JI = KX(J)
      IN = IX(J) + 1
      GOTO(131,133,135,137,139,141,143,145,147,149), IN
131   DU 132 I = 1, N
      IF (.NOT. CHKN ) GOTO 1310
      IF(X(I,J1).GT.0.0)GOTO 1310
      IF(NRE.GE. I) NRE = I - 1
      GOTO 151
1310 CONTINUE
      XMAN(I,J)=ALOG10(X(I,J1))
132 CONTINUE
133 MMITE(LP,41)J,(NAMX(I,J1),I=1,2),IX(J)
      GOTO 55
133   DU 134 I = 1, N
      XMAN(I,J)=X(I,J1)
134 CONTINUE
      GOTO 151
135 DU 136 I = 1, N
      XMAN(I,J)=X(I,J1)**2
136 CONTINUE
      GOTO 151
137 DU 138 I = 1, N
      XMAN(I,J)=X(I,J1)**3
138 CONTINUE
```

```
139      GOTO 151
140      DU      140 I = 1, N
141      XMAN(I,J)=X(I,J1)**4
142      CONTINUE
143      GOTO 151
144      IF ( (.NOT. CHKN) ) GOTO 1410
145      IF(X(I,J1),NE,0.0)GOTO 1410
146      IF(NRE .GE. I) NRE = I - 1
147      GOTO 151
148      CONTINUE
149      XMAN(I,J)=1.0/X(I,J1)
150      GOTO 151
151      DU      142 I = 1, N
152      XMAN(I,J)=X(I,J1)**4
153      CONTINUE
154      GOTO 151
155      IF ( (.NOT. CHKN) ) GOTO 1430
156      IF(X(I,J1),NE,0.0)GOTO 1430
157      IF(NRE .GE. I) NRE = I - 1
158      GOTO 151
159      CONTINUE
160      XMAN(I,J)=1.0/X(I,J1)**2
161      GOTO 151
162      DU      144 I = 1, N
163      XMAN(I,J)=X(I,J1)**2
164      CONTINUE
165      GOTO 151
166      IF ( (.NOT. CHKN) ) GOTO 1450
167      IF(X(I,J1),GT,0.0)GOTO 1450
168      IF(NRE .GE. I) NRE = I - 1
169      GOTO 151
170      CONTINUE
171      XMAN(I,J)=ALOG10(X(I,J1))
172      CONTINUE
173      GOTO 151
174      DU      146 I = 1, N
175      XMAN(I,J)=EXP(X(I,J1))
176      CONTINUE
177      GOTO 151
178      DU      148 I = 1, N
179      XMAN(I,J)=EXP(-X(I,J1))
180      CONTINUE
181      GOTO 151
182      CONTINUE
183      IF (NRE .LE. 0) GOTO 207
184      WRITE(LP,160) NRE
185      FORMAT('//11X,'THIS RUN WILL CONSIDER',I4,' VALID POINTS')
186      CALL REGRES(XMAN,XMAN,NRE,LIM,NPR,ERR)
187      IF( ERR ) GOTO 98
188      WRITE(LP,87)NRUN
189      FORMAT('//11X,'END OF RUN NO.',I5//11X,19('=-'))
190      NRUN = NRUN + 1
191      GOTO 24
192      WRITE(LP,90)NRUN
193      FORMAT('//11X,'*** REGRESSION CANNOT BE PERFORMED'
194      '6/15X,'WITH THESE DATA !')//11X'*** RUN NO.',I4,
195      '21 IS SKIPEO')
196      GOTO 88
197      RETURN
198      WRITE(LP,203)
199      READ(CR,7,END=5)FORM
200      GOTO 201
201      WRITE(LP,208)
202      WRITE(LP,204)LIM,KY,IY,(KX(I),IX(I),I=1,LIM)
203      GOTO 88
204      FORMAT('//1      *** WRONG <N> OR <K>')
205      FORMAT('//1      *** WRONG RUN PARAM.'//4X,13,(T7,7(15,12)))
```

```
205  WRITE(LP,206)
206  FORMAT(//'* *** WRONG DATA!//')
207  GOTO 201
208  FORMAT(//'* *** WRONG ASSOCIATION OF RUN PARAMETERS!')
209  END
* SEGMENT GRAMAT,VALORI
      SUBROUTINE CHKCONEX (ERR, GV)
C
      COMMON /GRAMAT/ WMAT(50,50),GMAT(50,50)
      COMMON /VALORI/ X(100,50),Y(100),IGR(50),NGR(50),LGR(50)
      SCON(3),SD(100,3),TEST(2,50),NM
      DIMENSION GV(3)
      LOGICAL*1 WMAT,GMAT,REJ,SCON,CONEX
      LOGICAL*1 ER,ERR
      LOGICAL*1 GV
C
      ERR = .FALSE.
      DO 100 I = 1, 3
C
      GV(I) = .FALSE.
      IG = I - 2
      NF = 0
      NN = 0
C
      DO 90 J = 1, M
C
      IF(LGR(J) .NE. IG) GOTO 70
      DO 60 K = 1, M
C
      IF(LGR(K) .NE. IG) GOTO 50
      WMAT(J,K) = GMAT(J,K)
      GOTO 60
      WMAT(J,K) = .FALSE.
50
      CONTINUE
C
      NN = NN + 1
      IF(NF .NE. 0) GOTO 90
      NF = J
      GOTO 90
C
      DO 80 K = 1, M
C
      WMAT(J,K) = .FALSE.
C
      CONTINUE
C
      SCON(I) = CONEX ( NF, NN, ER )
C
      IF (.NOT. ER) GOTO 100
C
      ERR = .TRUE.
      GV(I) = .TRUE.
C
100  CONTINUE
C
      RETURN
      END
* SEGMENT GRAMAT
      FUNCTION CONEX ( NF, NN, ERR )
      COMMON /GRAMAT/ CONNECT(50,50),GMAT(50,50)
```

```
DATA NNM /50/
LOGICAL*1 CONEX, CONNECT, MARK(50)
LOGICAL*1 STAR(50), ARROW(50), KMNS, GMAT
LOGICAL*1 ERR

C
ERR = .FALSE.
IF(NN.GT.1) GOTO 10
IF (.NN.EQ.0 ) GOTO 9
CONEX = .TRUE.
RETURN
9
CONEX = .TRUE.
ERR = .TRUE.
RETURN
10
CONTINUE

C
DO 1 I = 1, NNM
MARK(I) = .FALSE.
STAR(I) = .FALSE.
1
ARROW(I) = .FALSE.
MARK(NF) = .TRUE.
STAR(NF) = .TRUE.
ARROW(NF) = .TRUE.
DO 2 I = 1, NNM
IF(.NOT.CONNECT(I, NF)) GOTO 2
MARK(I) = .TRUE.
STAR(I) = .TRUE.
2
CONTINUE
CONEX = .FALSE.
3
CONTINUE
DO 5 I = 1, NNM
IF(.NOT.(MARK(I).AND.STAR(I).AND.,NOT.ARROW(I))) GOTO 5
ARROW(I) = .TRUE.
DO 4 J = 1, NNM
IF(.NOT.CONNECT(J, I)) GOTO 4
MARK(J) = .TRUE.
4
CONTINUE
5
CONTINUE
KMNS = .FALSE.
DO 6 I = 1, NNM
IF(.NOT.(MARK(I).AND.,NOT.STAR(I))) GOTO 6
KMNS = .TRUE.
STAR(I) = .TRUE.
6
CONTINUE
IF(KMNS) GOTO 3
NCARD = 0
DO 8 I = 1, NNM
IF(MARK(I).AND.STAR(I).AND.ARROW(I)) GOTO 7
IF(MARK(I).OR.,STAR(I).OR.ARROW(I))STOP 'TEST IN ERROR'
GOTO 8
8
NCARD = NCARD + 1
CONTINUE
IF (.NCARD.EQ. NN ) CONEX = .TRUE.
RETURN
END

* SEGMENT VALORI
SUBROUTINE SDCSDW(IR)

C
COMMON /VALORI/ X(100,50),Y(100),IGR(50),NGR(50),LGR(50)
1 SCUN(3),SD(100,3),TEST(2,50),N,M
2 DIMENSION SD(100),SDW(100)
3 DIMENSION SDWSQ(100)
EQUIVALENCE (SD(1,1),SDC(1))
EQUIVALENCE (SD(1,2),SDW(1))
EQUIVALENCE (SD(1,3), SDWSQ(1))
```

```
C      DO 20 I = 1, N
C      SDC(I) = 0.0
C      SDW(I) = 0.0
C      SDW3W(I) = 0.0
C
C      DO 10 J = 1, M
C      IF(LGR(J) .GT. 0) SDW(I) = SDW(I) + X(I,J) * LGR(J)
C      IF(LGR(J) .LT. 0) SDC(I) = SDC(I) + X(I,J) * LGR(J)
C10    CONTINUE
C20    CONTINUE
C
C      DO 30 I = 1, N
C      SUMSQ(I) = SDW(I) ** 2
C      IF(IR.EQ.1) SDW(I) = SDC(I) ** 2
C30    CONTINUE
C      RETURN
C      END
* SEGMENT REGPAR
SUBROUTINE REGRES(Y,X,N,L,NPR,VER)
COMMON /REGPAR/ BETA(21),f(21),SEREC(21),R,S,F
1,EXPYAR,SERY,SERES
2,VEPS
1 DIMENSION Y(100),X(100,L),Q(100),YR(100),XS(20)
1,XSSW(20),XYS(20),XM(20),A(21,22)
1,DIMENSION AA(21,22)
1,DOUBLE PRECISION AA,BETA,VEPS
1,LOGICAL*1 ER, NPR, VER
C
C      REGRESSION
*****  

C
C      VER = FALSE,
C      YS = X$IGMA(1,N)
C      YSSW = XYSIGMA(Y,Y,N)
C      DO 20 J = 1, L
C          DO 10 I = 1, N
C              Q(I) = X(I,J)
C10    CONTINUE
C      XS(J) = XSIGMA(Q,N)
C      XSSQ(J) = XYSIGMA(Q,Q,N)
C      XTS(J) = XYSIGMA(Q,Y,N)
C20    CONTINUE
C      FLN = FLOAT(N)
C      FLK = FLOAT(L)
C      ND = L + 1
C      NDPL = ND + 1
C      DO 30 I = 1, ND
C      DO 30 J = 1, ND
C          A(I,J) = 0.0
C30    CONTINUE
C      A(1,NDPL) = YS
C      A(1,1) = FLN
C      DO 40 I = 2, ND
C          J = I - 1
C          A(I,NDPL) = XYS(J)
C          A(1,I) = XS(J)
C          A(I,1) = XS(J)
C40    CONTINUE
```

```

40 CONTINUE
DO 52 I = 2, ND
   11 = I - 1
      DO 51 J = 2, ND
         J1 = J - 1
            DO 50 IP = 1, N
               A(I,J) = A(I,J) + X(IP,I1) * X(IP,J1)
                  CONTINUE
                     CONTINUE
CONTINUE

THE INTERCORRELATION MATRIX
***** *****
CCCCC
IF ( NRP ) GOTO 200
PRINT 60
FORMAT(' /T10, !REGRESSION RESULTS! //'
1/T10, !INTERCORRELATION MATRIX: > INDEX 1 IS (Y) !/')
IF ( ND .LE. 10) GOTO 130
PRINT 70, (I, I = 1, ND)
FORMAT(' /9X,20I6/')
DO 110 I = 1, ND
IM = I - 1
IF (I .NE. 1) GOTO 90
WT1 = 1.0
UU 80 J = 2, ND
JM = J - 1
W(J) = (FLN * XYS(JM) - YS * XS(JM)) /
1 SQRT((FLN * YSSQ - YS * YS) *
2 (FLN * XSSQ(JM) - XS(JM) ** 2))
CONTINUE
GOTO 101
90 W(1) = (FLN * XYS(IM) - YS * XS(IM)) /
1 SQRT((FLN * YSSQ - YS * YS) *
2 (FLN * XSSQ(IM) - XS(IM) ** 2))
UU 100 J = 2, ND
JM = J - 1
Q(J) = (FLN * A(I,J) - XS(IM) * XS(JM)) /
1 SQRT((FLN * A(I,I) - XS(IM) ** 2) *
2 (FLN * A(J,J) - XS(JM) ** 2))
CONTINUE
CONTINUE
PRINT 120, I,(Q(J), J = 1, ND)
CONTINUE
FORMAT(' /4X,I2,5X,20F6.2)
GO TU 200
PRINT 140, (I, I = 1, ND)
FORMAT(' /5X,10I12/')
DO 150 I = 1, ND
IM = I - 1
IF (I .NE. 1) GOTO 160
WT1 = 1.0
UU 150 J = 2, ND
JM = J - 1
Q(J) = (FLN * XYS(JM) - YS * XS(JM)) /
1 SQRT((FLN * YSSQ - YS * YS) *
2 (FLN * XSSQ(JM) - XS(JM) ** 2))
CONTINUE
GOTO 171
160 W(1) = (FLN * XYS(IM) - YS * XS(IM)) /
1 SQRT((FLN * YSSQ - YS * YS) *
2 (FLN * XSSQ(IM) - XS(IM) ** 2))

```

```
DO 170 J = 2, ND
    JM = J - 1
    Q(J) = (FLN * A(I,J) - XS(IM) * XS(JM))/
1      SQRT((FLN * A(I,I) - XS(IM) ** 2) *
2      (FLN * A(J,J) - XS(JM) ** 2))
170  CONTINUE
171  CONTINUE
    PRINT 190, I, (Q(J), J = 1, ND)
```

```
180  CONTINUE
190  FORMAT(' 1/4X,I2,6X,10(F8.4,4X))
C
C
C   REGRESSION COEFICIENTS
C
C   ***** *****
200  CONTINUE
    DO 202 I = 1, ND
        DO 201 J = 1, NDPL
            AA(I,J) = A(I,J)
201  CONTINUE
202  CONTINUE
    CALL CROUT (AA,BETA,ND,ER,VEPS)
    IF (ER) GOTO 320
    DO 210 I = 1, N
        YR(I) = BETA(1)
210  CONTINUE
    DO 230 J = 1, L
        DO 220 I = 1, N
            YR(I) = YR(I) + BETA(J+1) * X(I,J)
220  CONTINUE
230  CONTINUE
    DO 240 I = 1, N
        W(I) = Y(I) - YR(I)
240  CONTINUE
    YM = YS / FLN
    YMR = XSIGMA(YR,N) / FLN
    DO 250 I = 1, L
        XM(I) = XS(I) / FLN
250  CONTINUE
    SFN = XYSIGMA(Q,Q,N)
    R1 = 0.0
    R2 = 0.0
    R3 = 0.0
    DO 260 I = 1, N
        R1 = R1 + (Y(I) - YM) * (YR(I) - YMR)
        R2 = R2 + (Y(I) - YM) ** 2
        R3 = R3 + (YR(I) - YMR) ** 2
260  CONTINUE
C
C   GLOBAL PARAMETERS
C   **** *****
C   OF THE REGRESSION
C   **** *****
C
C
C   R = K1 / SQRT(R2 * R3)
C   S = SFN / (FLN - 1.0)
C   S = SQRT(S)
C   F = (FLN - FLK - 2.0) * R * R /
1     (FLK + 1.0) / (1.0 - R * R)
    EXPVAR = 1.0 - (SFN / (FLN - FLK - 1.0))
```



```
C/103 FORMAT(1      N=1,I4,1  V=1,G10.4)
      IF( N .GT. 1) GOTO 3
      IF( N .LT. 1) GOTO 12
      BETA(1) = A(1,2) / A(1,1)
      RETURN
3      DO 9 K = 1, NMIN
      KPL = K + 1
      L = K
      DO 4 I = KPL, N
         IF( A(I,K)*I*2 .GT. A(L,K) ** 2 ) L = I
4      CONTINUE
      IF( L .EQ. K) GOTO 6
      DO 5 J = K, NPL
         PHANTOM = A(K,J)
         A(K,J) = A(L,J)
         A(L,J) = PHANTOM
5      CONTINUE
6      DO 8 I = KPL, N
         IF( A(K,K) ** 2 .LE. V ) GOTO 13
         COM = A(I,K) / A(K,K)
         DO 7 J = KPL, NPL
            A(I,J) = A(I,J) - COM * A(K,J)
7      CONTINUE
8      CONTINUE
9      CONTINUE
      IF( (A(N,N) ** 2 .LE. V ) GOTO 14
      BETA(N) = A(N,NPL) / A(N,N)
      I = NMIN
10     IPL = I + 1
      S = 0.0
      DO 11 J = IPL, N
         S = S + A(I,J) * BETA(J)
11     CONTINUE
      IF( (A(I,I) ** 2 .LE. V ) GOTO 15
      BETA(I) = (A(I,NPL) - S) / A(I,I)
      I = I + 1
      IF( I .GE. 1) GOTO 10
      RETURN
12    CONTINUE
13    CONTINUE
14    CONTINUE
15    CONTINUE
      ER = .TRUE.
      RETURN
END
FUNCTION XSIGMA(X,N)
DIMENSION X(N)
XSIGMA = 0.0
DO 1 I = 1, N
   XSIGMA = XSIGMA + X(I)
1 CONTINUE
RETURN
END
FUNCTION XYSIGMA(X,Y,N)
DIMENSION X(N),Y(N)
XYSIGMA = 0.0
DO 1 I = 1, N
   XYSIGMA = XYSIGMA + X(I) * Y(I)
1 CONTINUE
RETURN
END
```

INPUT DATA FOR SIBIS

221	1	121	1 1 1 1 1	12	12	1
231	1	121	1 1 1 1 1		12	1 1
241	1	1	1 1 1 1 1 1	12		1
251	1		1 1 1 1 1 1		1 1 1 1	
261	1		1 1 1 1 1 1 12	12	1	"X"
271	1		1 1 1 1 1 1		1	(continued)
281	1		1 1 1 1 1 1		1 1	
291	1		1 1 1 1 1 1		1	
301	1		1 1 1 1 1 1	8	1	
311	1		1 1 1 1 1 1	12	1	
321	1		1 1 1 1 1 1	13	1	
331	1		1 1 1 1 1 1 17		1	
341	1		1 1 1 1 1 1 12	12	1	
↓						
EOF ← end of data (for X)						
6/2/20/ ← vertex 1, type "c" connected with 2 vertices, 2C 3 1 3 !						
3C 2 2 4						
4C 3 3 5 6						
5W 3 4 6 14						
6/4/4/5/11/ ← vertex 6, type "c" connected with 4 vertices, 7C 3 2 6 8						
8C 3 7 9 19 9C 3 8 10 18						
⟨IRS⟩ - input FORMAT - (I2,A1,(38I2))						
10C 4 9 11 15 16						
11C 3 6 10 14						
12W 3 1 1 1 3 14						
13W 2 1 2 1 4						
14W 3 5 1 2 1 3						
15W 2 1 0 1 6						
16W 4 1 0 1 5 1 / 24						
17W 3 1 6 1 8 2 4						
18W 3 9 1 7 2 4						

19W 3 1 824  
20W 2 121  
21W 22022  
22W 22123  
23W 22224  
24I 51617181923

↑  
**IRS** - (continued)  
↓

.EOF — end of data (for SIBIS-LV)  
SIBIS-NL { (it was a complete set of input data)  
          SIBIS + Non Linear version  
          (AVY = AVX = AVIGR = .FALSE.  
          The run will be performed  
          with the same input data).

- For HIBIS, input data have the same structure.

INPUT DATA FOR POLYREG  
POLYFUNCTIONAL REGRESSION ANALYSIS

POLYREG      HI-AIB }  
N      \*\*\*\*\* } ← TITLE of the regression  
10 5←M

HI      L .      B1      B2      B3      B4 } ← variables  
(6F5.3) ← input FORMAT for (X(I,J),J=1,M+1)

447 3	152	19	19	204	"X" - each card is a row
1023 411	152	19	19	297	
1523 505	152	19	19	349	
1154 411	204	276	316	316	
2023 617	152	19	19	442	
1951 505	152	19	316	421	
1879 505	19	276	316	349	
1724 411	259	286	286	297	
2253 711	152	19	19	494	
2379 617	152	19	316	442	

T 1 11 21 ← This RUN parameters card means:  
T 1 11 31      RUN PARAMETERS      - DATA will be verified;  
T 1 11 41      - monoparametric regression;  
T 1 11 51      - "Y" is "HI"  
T 1 11 61      - "X" is "B1"

.EOF ← end of run parameters - new data are required under      the same TITLE  
.EOF ← end of data under this TITLE  
.EOF ← end of data for POLYREG

after this ".EOF" card, one can ask a new computation specifying a keyword and a new data set, or finish the execution of the program with a new ".EOF" card!

## APPENDIX 2

Teach the Computer to Recognize Connected Graphs.

The algorithm CONEX.

The algorithm is based on the idea that starting with a given vertex of a connected graph, one may reach any vertex of the graph.

For brevity, the algorithm is described in ALGOL.

```
function CONEX (G,K,N)
begin
  for i = 1 step 1 until N
    do
      begin
        V(m)[i] := false;
        V(*)[i] := false;
        V(t)[i] := false;
      end
    end
  V(m)[K] := true; V(*)[K] := true; V(t)[K] := true;
  for i = 1 step 1 until N
    do
      begin
        if G[i,K]
          then
            V(m)[i] := true;
            V(*)[i] := true;
        fi
      end
    end
  l: for i = 1 step 1 until N
    do
      begin
        if V(m)[i] & V(*)[i] & ~V(t)[i]
          then
            V(t)[i] := true;
```

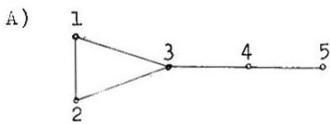
```
for j = 1 step 1 until N
do
begin
if G[i,j]
then
V[m][j] := true;
fi
end
end
fi
end
end
KNMS := false;
for i = 1 step 1 until N
do
begin
if V[m][i] & V[x][i]
then
KNMS := true;
V[m][i]:= true;
fi
end
end
if KNMS
then
go to 1;
else
CARD := 0;
for i = 1 step 1 until N
do
begin
if V[m][i] & V[x][i] & V[t][i]
then
CARD := CARD + 1;
fi
end
end
```

```

if CARD ≠ N
then
    return false;
else
    return true;
fi
end CONEX;

```

Illustratively, let us consider two applications of the algorithm:



$$G = (X, \Gamma); \text{ Card } X = 5$$

$$\begin{vmatrix} 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{vmatrix} = \begin{vmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{vmatrix}$$

The  $V^{[m]}$ ,  $V^{[*]}$  and  $V^{[t]}$  vectors, for each step, reads:

$\overline{V^{[t]}}$	$\overline{V^{[*]}}$	$\overline{V^{[m]}} \quad 0 \ 0 \ 0 \ 0 \ 0$	(start with the vertex 1)
$\Downarrow$			
$\overline{V^{[t]}} \quad \uparrow \ \uparrow$			$\overline{V^{[t]}} \quad \uparrow \ \uparrow \ \uparrow$
$\overline{V^{[*]}} \quad * \ *$			$\overline{V^{[*]}} \quad * \ * \ *$
$\overline{V^{[m]}} \quad 0 \ 1 \ 1 \ 0 \ 0$			$\overline{V^{[m]}} \quad 1 \ 1 \ 1 \ 0 \ 0$
			$\Downarrow$
$\overline{V^{[t]}} \quad \uparrow \ \uparrow \ \uparrow \ \uparrow$			$\overline{V^{[t]}} \quad \uparrow \ \uparrow \ \uparrow$
$\overline{V^{[*]}} \quad * \ * \ * \ *$			$\overline{V^{[*]}} \quad * \ * \ * \ *$
$\overline{V^{[m]}} \quad 1 \ 1 \ 1 \ 1 \ 0$			$\overline{V^{[m]}} \quad 1 \ 1 \ 1 \ 1 \ 0$
$\Downarrow$			

$\Rightarrow$

$\Leftarrow$

$$\begin{array}{c}
 \downarrow \\
 \begin{array}{rccccc}
 V^{[\dagger]} & \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\
 \hline
 V^{[*]} & * & * & * & * & * \\
 \hline
 V^{[m]} & 1 & 1 & 1 & 1 & 1
 \end{array}
 \end{array}
 \Rightarrow
 \begin{array}{rccccc}
 V^{[\dagger]} & \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\
 \hline
 V^{[*]} & * & * & * & * & * \\
 \hline
 V^{[m]} & 1 & 1 & 1 & 1 & 1
 \end{array}$$

There is no entry of  $V^{[m]}$  equal to 1 with corresponding  $V^{[*]}$  and  $V^{[\dagger]}$  entries different from \* and  $\uparrow$ , respectively. The computing procedure is stopped, and one totalizes the 1's of the  $V^{[m]}$ :

$$\sum V^{[m]} = 5 = \text{Card } X \Rightarrow \text{the graph } G \text{ is connected.}$$

B)

$$G = (X, \Gamma); \quad \text{Card } X = 4.$$

$$\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}$$

$$\begin{array}{r}
 \hline
 V^{[\dagger]} \\
 \hline
 V^{[*]} \\
 \hline
 V^{[m]} & 0 & 0 & 0 & 0
 \end{array}
 \quad (\text{start with the vertex 2})$$

$$\begin{array}{c}
 \downarrow \\
 \begin{array}{rcc}
 V^{[\dagger]} & \uparrow & \\
 \hline
 V^{[*]} & * & \\
 \hline
 V^{[m]} & 1 & 0 & 0 & 0
 \end{array}
 \end{array}
 \Rightarrow
 \begin{array}{rcc}
 V^{[\dagger]} & \uparrow & \uparrow \\
 \hline
 V^{[*]} & * & * \\
 \hline
 V^{[m]} & 1 & 1 & 0 & 0
 \end{array}$$

$$\begin{array}{rcc}
 V^{[\dagger]} & \uparrow & \uparrow \\
 \hline
 V^{[*]} & * & * \\
 \hline
 V^{[m]} & 1 & 1 & 0 & 0
 \end{array}$$

$\sum V^{[m]} = 2 \neq \text{Card } X = 4;$   
so:  
the graph  $G$  is not connected.